Atomic Weights—No Longer Constants of Nature

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Many of us grew up being taught that the standard atomic weights we found in the back of our chemistry textbooks or on the Periodic Table of the Chemical Elements hanging on the wall of our chemistry classroom are constants of nature. This was common knowledge for more than a century and a half, but not anymore. The following text explains how advances in chemical instrumentation and isotopic analysis has changed the way we view atomic weights and why they are no longer constants of nature.

Atomic Weight

The concept of atomic weights goes back to the time of John Dalton at the beginning of the nineteenth century. Much of chemistry in the first half of that century involved the measurement and analysis of atomic weights. Many scientists, most notably Dmitri Mendeleev, analyzed and divided the atomic weights of the elements into triads, octaves, and spirals, based on similarities of the chemical and physical properties of these elements. Mendeleev provided a periodic table along with predictions of new elements to fill gaps in his table, and these elements subsequently were discovered. In 1882, Frank W. Clarke recommended atomic-weight values for use in science, industry, and trade.¹ The American Chemical Society assigned Clarke to annually issue atomic weight tables as a one-man committee. Other countries created similar committees and the values of these atomic-weight tables often differed. An international commission was called for by the German Atomic Weights Commission. A first report of the International Commission on Atomic Weights (ICAW) for 1901 was published as a flyleaf in issue 1 of the Chemische Berichte in January 1902.² In 1913, the Commission became part of the International Association of Chemical Societies (IACS), which was dissolved following World War I but the Commission continued to publish updated Tables of Atomic Weights each year until 1921–1922. In 1919, the International Union of Pure and Applied Chemistry (IUPAC) was created as the chemical section of the International Research Council. An atomic-weight report from a new Commission, under IUPAC auspices, was first prepared in 1925. Since that time, ICAW or its successors within IUPAC, hereafter termed the Commission, took over the careful evaluation and dissemination of atomic-weight values, which continued to be considered as “constants of nature.”

Isotopes

A constant of nature, such as the Faraday constant [96 485.3399(24) C mol⁻¹], typically is known to better than 1 part in a million parts. IUPAC’s Periodic Table³ lists a value of 10.811(7) for boron. If standard atomic weights are constants of nature, why are the values not published with greater accuracy? The answer, of course, is that the atomic weight of an element depends upon the source of the material and upon its number of stable isotopes, where isotopes are atoms of the same element having different mass numbers. At the start of the twentieth century, radioactive elements were discovered. Fredrick Soddy showed the chemical identity of meso-thorium (²²⁸Ra) and radium (²²⁶Ra).⁴ He concluded that these were chemical elements with different radioactive properties and with different atomic weights, but with the same chemical properties and should
occupy the same positions in the Periodic Table of the Elements. He coined the word isotope (Greek: in the same place) to account for radioactive species. An event that profoundly affected atomic weights was the discovery by John (J. J.) Thomson in 1912 that the element neon was made up of two stable isotopes, \(^{20}\text{Ne}\) and \(^{22}\text{Ne}\). \(^{21}\text{Ne}\) was discovered later. With the discovery of stable isotopes and the use of mass spectrographs to measure the isotopic composition of chemical elements, it was realized that the masses of the individual stable isotopes and their isotopic-abundance values (mole fractions) could provide an alternative method for estimating an element’s atomic weight. With technical improvements to mass spectrometers, the accuracy of this method began to exceed chemical determinations of the atomic weight. Over the last half of the Twentieth Century, almost every new recommended atomic-weight value was based on mass spectrometric measurements.

**Variations in abundances of isotopes and atomic weights**

In 1908, the atomic weight of “common” lead (from a non-radioactive source material) was measured to be 207.2, while a 1914 measurement of lead from a thorium silicate mineral had an atomic weight of 208.4. A low value of 206.4 was measured for the atomic weight of lead in uranium samples in 1914. Differences in lead atomic weight values were considered to be an exceptional case that was attributed to lead isotopes being products of the natural radioactive decay chains. However in 1936, Malcolm Dole reported the variation of oxygen’s atomic-weight value in air and in water because of variations in abundances of its stable isotopes. In 1939, Alfred O.C. Nier reported on the 5% variation in the isotopic composition of carbon. It was becoming clear that atomic weights might not be constants of nature. In the Commission’s meeting in 1951, it was recognized that the isotopic-abundance variation of sulfur impacted the internationally accepted value of an atomic weight. In order to indicate the span of values that may apply to sulfur from different natural sources, the value ± 0.003 was attached to the atomic weight of sulfur. Ranges were listed for six elements (H, B, C, O, Si, and S) due to the natural variation in their isotopic compositions, and experimental uncertainties were added for an additional five elements (Cl, Cr, Fe, Br, and Ag) in the 1961 report of the Commission. In the 1969 report of the Commission, uncertainties were added for all atomic-weight values for the first time. IUPAC had now added to its responsibilities, the careful evaluation and dissemination of atomic-weight uncertainties, derived from critically-assessed, published information. Also in the 1969 report, the Commission acknowledged for the first time that:

“The discovery that most chemical elements exist in nature as isotopic mixtures, many of which are known to vary in composition, makes it necessary to modify the historical concept of atomic weights as constants of nature. Even though [stable] isotopes have not been observed in nature for some elements (currently 21 in number), it appears more logical to consider that isotopic mixtures represent the normal rather than the exceptional state of an element. The Commission considers that this attitude will promote an awareness that uncertainties in the values given in the International Table are no longer, as in earlier times, to be regarded as resulting only from errors in the measurement of the value, but that they arise from natural variations in isotopic composition. To arrive at the recommended value for the atomic weight the Commission will use weighting procedures so that the value will be optimized for materials in world science, chemical technology and trade, rather than represent an estimated geochemical average.”
Not all elements, though, exhibit variations in their atomic weights; some have only one stable isotope. Determination of the standard atomic weights of the 21 elements with a single stable isotope\textsuperscript{15}, such as F, Al, Na, and Au, is relatively simple because they depend only upon the atomic mass of a single stable isotope. These standard atomic weights are constants of nature and their values are known to better than one part in a million parts.

Due to the growing importance of isotopic measurements for atomic weights, the Commission changed its name in 1979 to Commission on Atomic Weights and Isotopic Abundances. The Commission decided that an atomic weight could be defined for any specified sample. For the IUPAC table of recommended values of atomic weights, the Commission decided that\textsuperscript{16}:

“Dated Tables of Standard Atomic Weights published by the Commission refer to our best knowledge of the elements in natural terrestrial sources.”

Atomic-weight distributions determined from published variations in isotopic compositions can span relatively large intervals. Fig. 1 shows the variation in atomic weight as a function of mole fraction of \textsuperscript{2}H in selected hydrogen-bearing materials. The atomic weight of hydrogen in “normal” materials spans atomic-weight values from approximately 1.00785 to 1.00798,\textsuperscript{17,18} whereas the uncertainty of the atomic weight calculated from the best measurement of the isotopic abundance of hydrogen\textsuperscript{19} is about a thousand times smaller; \( A_r(\text{H}) = 1.007\ 981\ 75(5) \). By a “normal” material, the Commission means a material from a terrestrial source that satisfies the following criterion\textsuperscript{20}:

“The material is a reasonably possible source for this element or its compounds in commerce, for industry or science; the material is not itself studied for some extraordinary anomaly and its isotopic composition has not been modified significantly in a geologically brief period.”

To determine the atomic-weight value of an element having variations in the abundances of its stable isotopes in natural materials that result in a span of atomic-weight values (e.g., H, Li, B, C, N, etc.), the Commission typically has evaluated published variations in isotopic compositions, selected an atomic weight near the median value as the standard atomic weight, and assigned an uncertainty to encompass most or all of the published atomic-weight values. For example, for hydrogen (Fig. 1) the Commission selected at its 1981 meeting\textsuperscript{21} a standard atomic-weight value of 1.007 94 with an uncertainty of 0.000 07. The Commission’s concern that the chemical community would have difficulty in handling asymmetric uncertainties and that most computer programs would not be able to treat asymmetric uncertainties properly led the Commission to always adopt symmetric uncertainties for standard atomic-weight values, even in cases where asymmetric uncertainties were called for. This presentation method is unsatisfactory for several reasons.

1. Students and others commonly misinterpret the uncertainty value of the standard atomic weight as a measurement uncertainty, and they wonder why standard atomic weights cannot be determined more accurately.

2. In years following the determination of a new standard atomic weight, newly published natural variations provide atomic weight values that commonly exceed the bounds of the newly adopted standard atomic-weight value; thus, standard atomic weight needed to be changed regularly or they did not reflect recently published scientific literature.
3. The standard atomic-weight value is commonly expected by readers to reflect a Gaussian distribution, and it does not reflect satisfactorily the bimodal distribution of some elements, for example, boron and sulfur.\textsuperscript{17,18}

4. It is often difficult, or even impossible, to find a material with an atomic-weight value identical to the standard atomic weight. For example, finding a hydrogen-bearing material with an atomic weight of 1.007 94 would be a challenge.

Fig. 1. Variation in atomic weight with isotopic abundance of selected hydrogen-bearing materials\textsuperscript{17,18,22}. Isotopic reference materials are designated by solid black circles. The previous (2007) standard atomic weight of hydrogen was 1.007 94(7). The atomic-weight uncertainty of the “best measurement” of isotopic abundance\textsuperscript{19} is approximately
±0.000 000 05, which is about 1,000 times smaller than the uncertainty of the 2007 standard atomic weight.\textsuperscript{23}

**Atomic-weight Intervals**

A new presentation method for standard atomic weights of elements such as H, Li, B, C, and N was needed. At its meeting in 2009 in Vienna, the Commission decided to express the standard atomic weight of hydrogen and nine other elements in a manner that clearly indicates that the values are not constants of nature.\textsuperscript{24} The span of atomic-weight values in normal materials is termed the interval. The interval is used together with the symbol \([a; b]\) to denote the set of values \(x\) for which \(a \leq x \leq b\), where \(b > a\) and where \(a\) and \(b\) are the lower and upper bounds, respectively.\textsuperscript{25} Neither the upper nor lower bounds have any uncertainty associated with them; each is a considered decision by the Commission based on professional evaluation and judgment. Writing the standard atomic weight of hydrogen as \([1.007 84; 1.008 11]\) indicates that the atomic weight in any normal material will be greater than or equal to 1.007 84 and will be less than or equal to 1.008 11. Thus, the atomic-weight interval is said to encompass atomic-weight values of all normal materials. The range of an interval is the difference between \(b\) and \(a\), that is \(b - a\).\textsuperscript{25} Thus, the range of the atomic-weight interval of hydrogen is calculated as 1.008 11 – 1.007 84 = 0.000 27.

The lower bound of an atomic-weight interval is determined from the lowest atomic weight determined by the Commission’s evaluations, taking into account the uncertainty of the measurement. Commonly, an isotope-delta measurement\textsuperscript{17,18} is the basis for the determination of the bound. In addition to the uncertainty in the delta measurement, the uncertainty in the atomic weight of the material anchoring the delta scale is also taken into account.\textsuperscript{17,18} If substance \(P\) is the normal terrestrial material having the lowest atomic weight of element \(E\), then

\[
\text{lower bound} = \text{lowest } A_r(E)_P - U[A_r(E)]_P
\]

where \(U[A_r(E)]_P\) is the combined uncertainty that incorporates the uncertainty in the measurement of the delta value of substance \(P\) and the uncertainty in relating the delta-value scale to the atomic-weight scale. For hydrogen, the substance with the lowest published, evaluated \(^2\)H abundance is hydrogen gas in a natural gas well,\textsuperscript{17,18} and for it \(A_r(H) = 1.007 8507\), and \(U[A_r(H)] = 0.000 0046\). Thus, the lower bound is 1.007 8461. The combined uncertainty constrains the number of significant figures in the atomic-weight value of the bound. For hydrogen, the sixth digit after the decimal point is uncertain; therefore, the value is truncated to 5 digits after the decimal point. For the lower bound of hydrogen, 1.007 8461 is truncated to 1.007 84. The upper bound is determined in an equivalent manner, but for an upper bound, the trailing digit is increased to ensure the atomic-weight interval encompasses the atomic-weight values of all normal materials. The lower and upper bounds are evaluated so that the number of significant digits in each is identical. If a value ends with a zero, it may need to be included in the value to express the required number of digits.
Elements whose atomic weights are now presented as intervals are shown below.\textsuperscript{24}

<table>
<thead>
<tr>
<th>Element name</th>
<th>From</th>
<th>To the interval</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hydrogen</td>
<td>1.007 94(7)</td>
<td>[1.007 84; 1.008 11]</td>
</tr>
<tr>
<td>Lithium</td>
<td>6.941(2)</td>
<td>[6.938; 6.997]</td>
</tr>
<tr>
<td>Boron</td>
<td>10.811(7)</td>
<td>[10.806; 10.821]</td>
</tr>
<tr>
<td>Carbon</td>
<td>12.0107(8)</td>
<td>[12.0096; 12.0116]</td>
</tr>
<tr>
<td>Nitrogen</td>
<td>14.0067(2)</td>
<td>[14.006 43; 14.007 28]</td>
</tr>
<tr>
<td>Oxygen</td>
<td>15.9994(3)</td>
<td>[15.999 03; 15.999 77]</td>
</tr>
<tr>
<td>Silicon</td>
<td>28.0855(3)</td>
<td>[28.084; 28.086]</td>
</tr>
<tr>
<td>Sulfur</td>
<td>32.065(5)</td>
<td>[32.059; 32.076]</td>
</tr>
<tr>
<td>Chlorine</td>
<td>35.453(2)</td>
<td>[35.446; 35.457]</td>
</tr>
<tr>
<td>Thallium</td>
<td>204.3833(2)</td>
<td>[204.382; 204.385]</td>
</tr>
</tbody>
</table>

In some cases, users may need a representative value for an element having an atomic-weight interval, such as for trade and commerce. Conventional atomic-weight values are conventional quantity values\textsuperscript{25}, and were provided by the Commission.\textsuperscript{24} For example, the conventional atomic-weight value for hydrogen is 1.008.

Figure 2 is an example from IUPAC’s isotopic periodic table for the educational community.\textsuperscript{26} The isotopic abundances of an element are shown in a pie diagram. This figure shows four classifications of elements: (a) those whose standard atomic weights are not constants of nature and are assigned an interval, (b) those whose standard atomic weights are not constants of nature and they are not assigned an interval, (c) those whose atomic weight is a constant of nature because they have a single stable isotope, and (d) those who have no standard atomic weight because they have no stable isotopes. This fundamental change in the presentation of the atomic weights represents an important advance in our knowledge of the natural world and will underscore the significance and contributions of chemistry to the well being of humankind in the International Year of Chemistry in 2011.
Fig. 2. Potential illustrations for elements in IUPAC’s new isotopic periodic table for the educational community\textsuperscript{26} with isotopic abundances shown as pie diagrams. \textbf{a.} Element (chlorine) whose standard atomic weight is \textbf{not} a constant of nature and is an interval. \textbf{b.} Element (mercury) whose standard atomic weight is \textbf{not} a constant of nature and is not an interval. \textbf{c.} Element (arsenic) whose standard atomic weight \textbf{is} a constant of nature because it has a single stable isotope. \textbf{d.} Element (americium) that has no stable isotopes and thus no standard atomic weight.
Guidelines for Atomic-weight Intervals

1. The variation in atomic-weight values, $A_r(E)$, of an element E is termed an atomic-weight “interval” with the symbol $[a; b]$, where $a$ and $b$ are the lower and upper bounds, respectively, of the interval; thus, for element E, $a \leq A_r(E) \leq b$.

2. The standard atomic weight of an element, expressed as an interval, $[a; b]$, should **not** be expressed as the average of $a$ and $b \pm$ half of the difference between $b$ and $a$.

3. The atomic-weight interval and range should not be confused. The atomic-weight range is equal to $b - a$, where $a$ and $b$ are the lower and upper bounds, respectively.

4. The lower and upper bounds commonly are determined from mass spectrometric measurements of normal materials, taking into account uncertainties of the measurements and taking into account the uncertainty of the “best measurement” of isotopic abundances of an element used to determine its 2007 standard atomic weight.

5. The atomic-weight interval encompasses atomic-weight values of all normal materials.

6. Both lower and upper bounds are consensus values, and neither has any uncertainty associated with it.

7. The atomic-weight interval is the standard atomic weight, which is the best knowledge of the atomic weights of natural terrestrial sources.

8. The number of significant figures in the lower and upper bounds are adjusted so that mass spectrometric measurement uncertainties do not impact the bounds.

9. The number of significant figures in the lower and upper bounds should be identical. A zero as a trailing digit in a value may be needed and is acceptable.

10. The atomic-weight interval is selected conservatively so that changes in the Table of Standard Atomic Weights are needed infrequently. Thus, IUPAC’s Commission on Isotopic Abundances and Atomic Weights may recommend additional conservatism and may reduce the number of significant figures.

11. The atomic-weight interval is given as precisely as possible and should have as many digits as possible, consistent with the previously stated rules.

12. Values of atomic-weight intervals are updated in the Table of Standard Atomic Weights by the Commission following completion of an IUPAC project reviewing the published literature for peer-reviewed isotopic abundance data.

13. If the variation in isotopic composition in normal materials of an element is under evaluation by an IUPAC project, a footnote “r” may be retained in the Table of Standard Atomic Weights until the project completes its evaluation in order that changes to the Tables are infrequent. Currently, such elements include He, Ni, Cu, Zn, Se, Sr, Ar, and Pb.
References